

# Inverse and hybrid approaches for disordered solids

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THAPA

# Logic...

*Modeling as a problem of inference*



*E. T. Jaynes*  
1922-1998

- 1) Conventional approach: Do your best simulation (big cell, fancy interactions, long simulation times, etc). *This is very different from the way the material was really made!* Compare to experiment, hope for the best. Write the paper.
- 2) There may be other information that would improve the realism of the simulation -- experimental, chemical or other information not included. *Why not use it in making the model?!*

# Modeling paradigms and imposing *a priori* information

- 1) **Simulation:** Implement your best calculation (big cell, fancy interactions, long time evolution, etc). Hope that the results look like experimental ones.
- 2) **Information:** Try to invert the experimental data.
- 3) **Merge the two:** carry out simulation but impose the *a priori* (possibly experimental) information as part of the simulation.

# Reverse Monte Carlo

Kaplow, McGreevy *et al.*

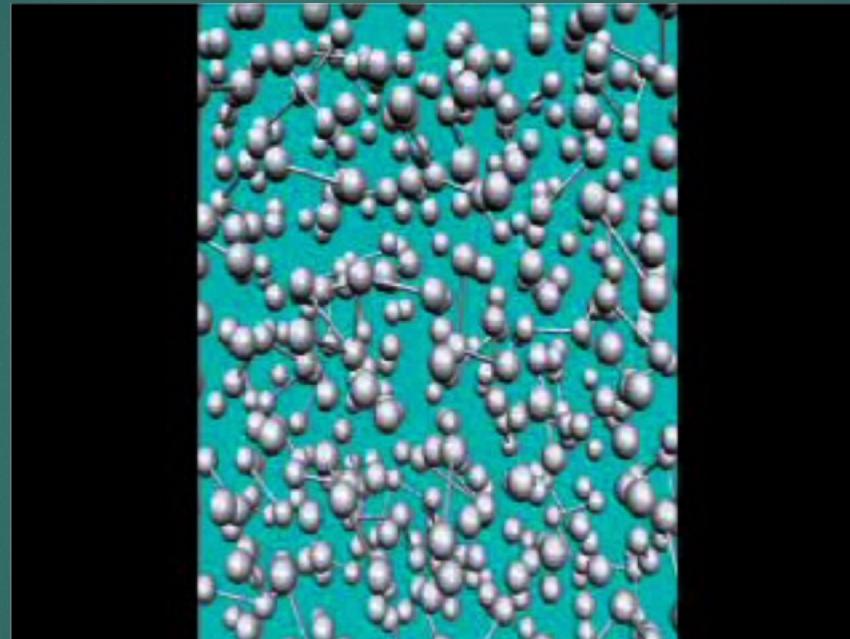
- ▶ **Information paradigm.** What does experiment imply about the structure?
- ▶ Reverse Monte Carlo: put atoms in a supercell, move at random with Monte Carlo, keep moves if closer to experiment, accept with Metropolis probability if worse.
- ▶ Result: matches experiment by construction, but diffraction data **alone** is **insufficient** to produce a chemically realistic model. Still, *it is a clever idea*  
-- ***use the information you have!***

# RMC: Discussion

- ▶ Promising **if** additional information (constraints) are employed.
- ▶ Flexible, enables inclusion of *a priori* information.
- ▶ Constraints are tricky: we are imposing information, but we are potentially imposing errors – *the model is only as good as the information employed!*

# RMC: order from chaos

RMC on a-Si (diffraction plus bond angle constraint)

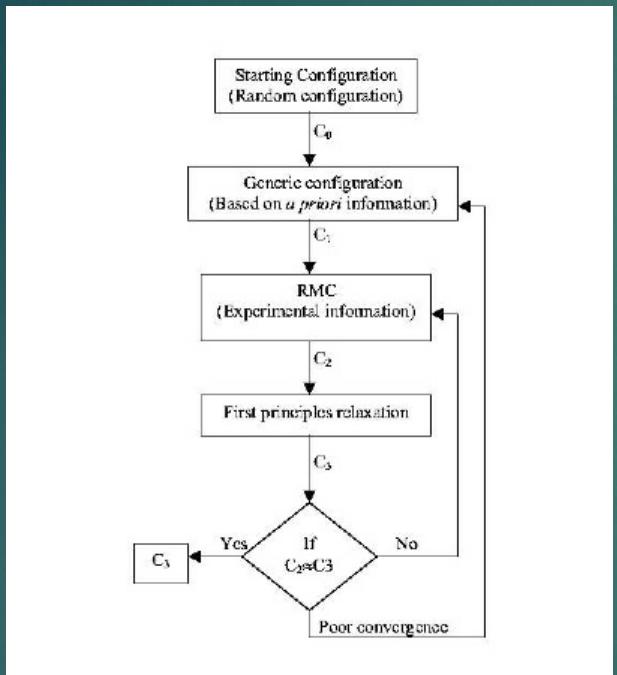


Credit: **Partha Biswas (about 2005)**

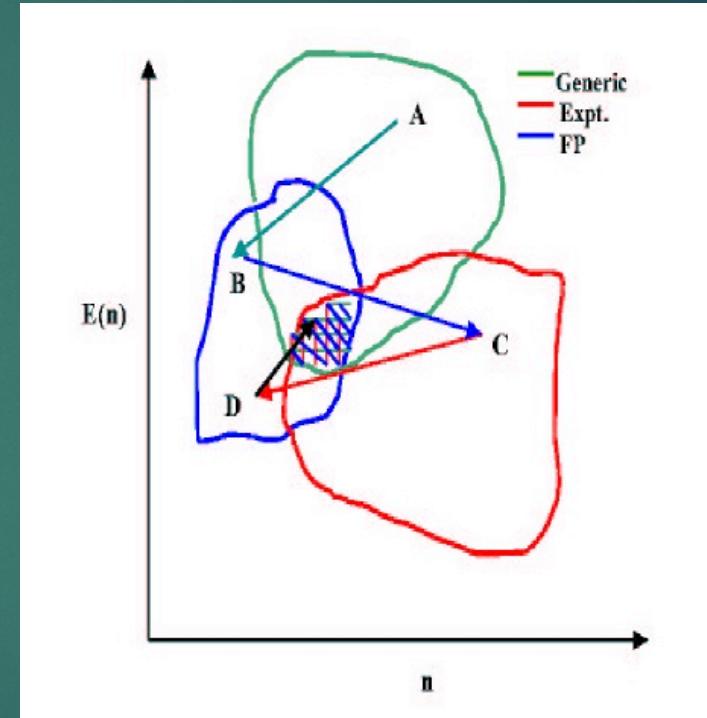
# Experimentally Constrained Molecular Relaxation (ECMR)

- ▶ We want to include experimental data in MD: **merge RMC and molecular dynamics modeling.**
- ▶ Start from experimentally realistic subspace, self-consistently iterate between RMC and first principles relaxation.

# ECMR: *implementation*



Flow chart for ECMR



Cartoon suggesting  
ECMR convergence

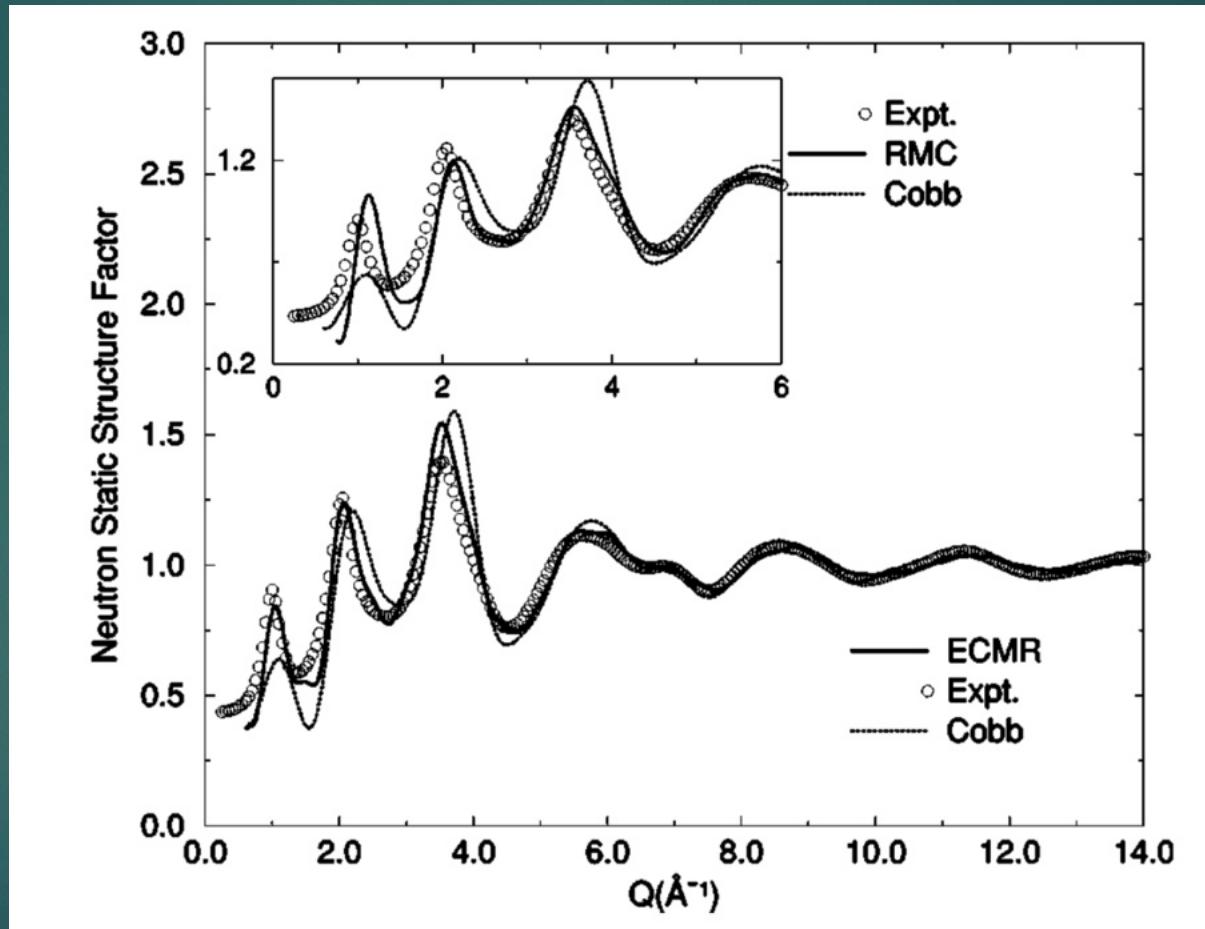
# ECMR & GeSe<sub>2</sub>

- ▶ GeSe<sub>2</sub>: Classic chalcogenide glass, hard to model well, especially first sharp diffraction peak.
- ▶ Lets try ECMR:

Experimental input: Petri and Salmon partial structure factors.

Hamiltonian: Density functional, minimal basis, supercell with 648 atoms in unit cell.

# ECMR: g-GeSe<sub>2</sub> results



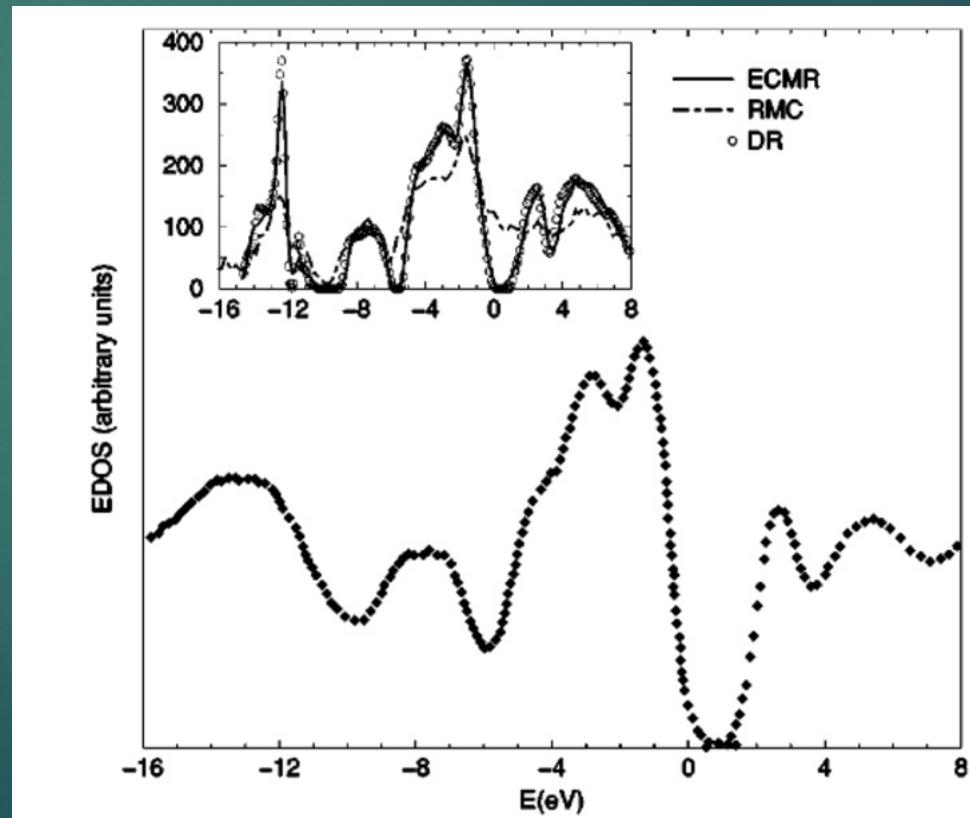
Static structure factor

# Electronic structure: density of states

Note: a valid structural model **must** have a realistic electronic DOS.

GeSe<sub>2</sub>

Expt: XPS - Bergignat *et al*  
PRB (1988), IPES- Hosokawa  
*et al*, JPCM (1994)



# ECMR: improving the convergence

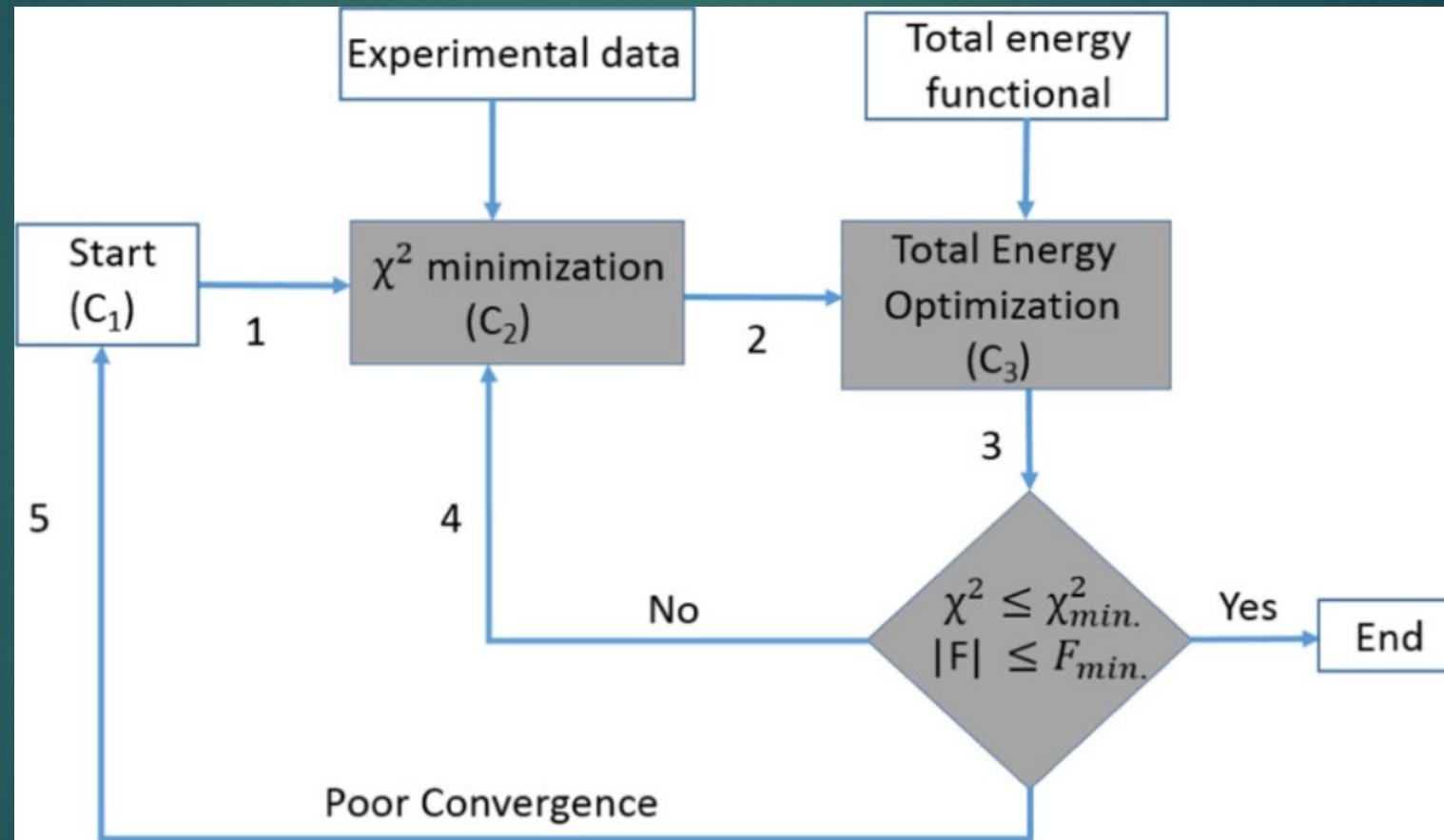
- ▶ ECMR is great – *if it converges!*
- ▶ Rather than doing a sequence of full relaxations, perform partial inversions, followed by partial relaxations.
- ▶ Iterate THAT!
- ▶ Seems to be more robust than ECMR.

# Beyond ECMR: Force Enhanced Atomic Refinement (FEAR)

- ▶ Start with random model (assume density is known)
- ▶ Repeat to these two steps convergence:
  - Obtain N accepted moves from RMC [drives model toward experiment]
  - Take M conjugate gradients steps with energy functional [enforce chemistry]

Typically  $N \sim 100$ ,  $M \sim 1-5$ . Always  $N \gg M$ .

# Force Enhance Atomic Refinement (FEAR)

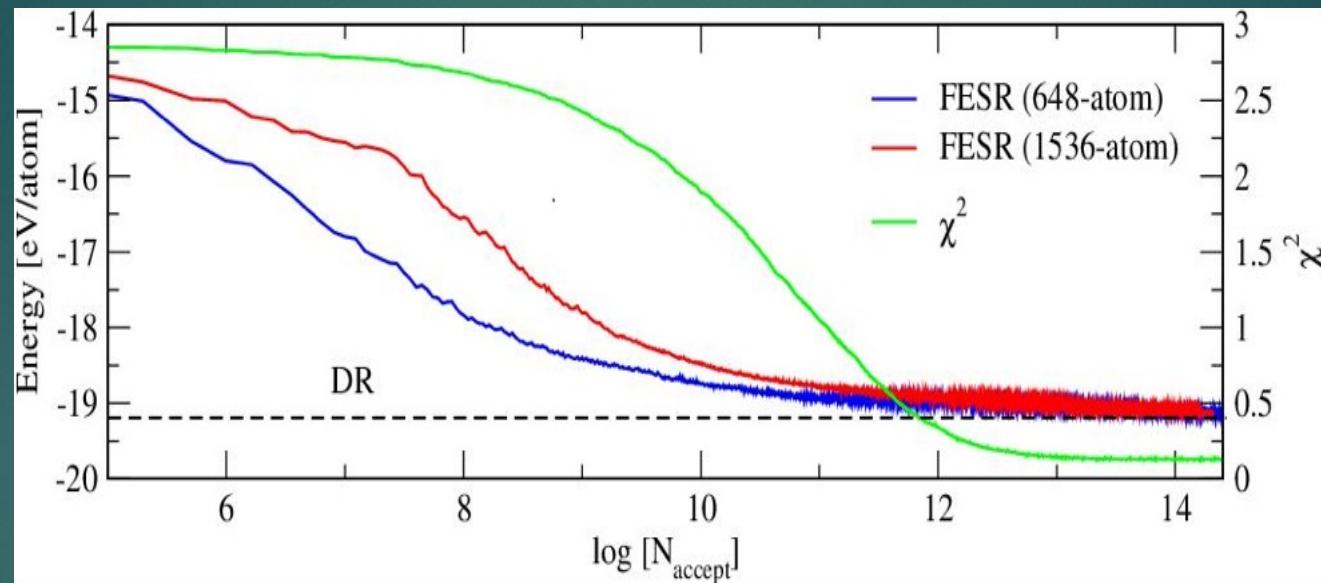


Pandey et. al, Phys.RevB 94, 235208 (2016)

# Example: FEAR for amorphous SiO<sub>2</sub>

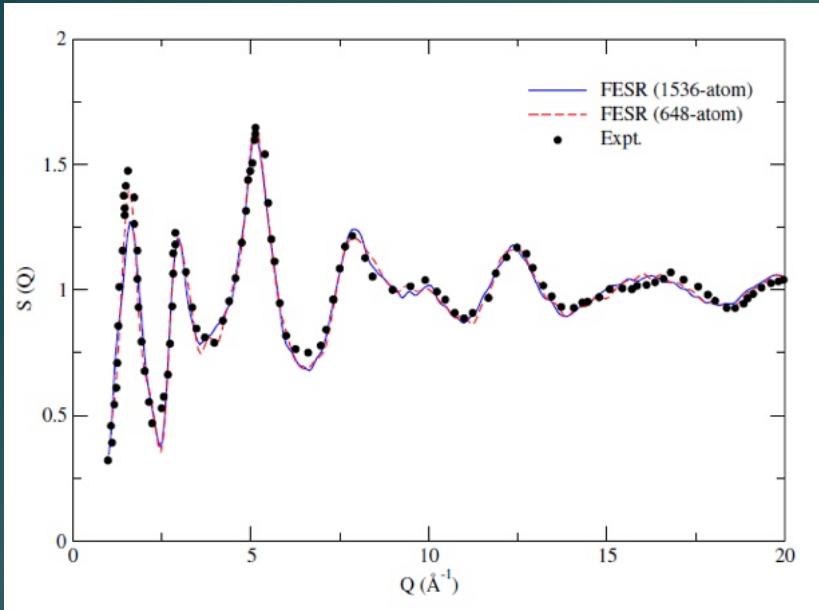
- ▶ Adopt 648-atom, 1536-atom models.
- ▶ Use the van Beest (BKS) potential (PRL, 1990). Start with **random** coordinates.
- ▶ After 100 successful RMC moves, move all the atoms along van Beest gradient – only one step, *not a full minimization*.
- ▶ *Repeat previous until convergence (fit and force) is achieved.*
- ▶ Need about 30,000 force calls

# FEAR of silica

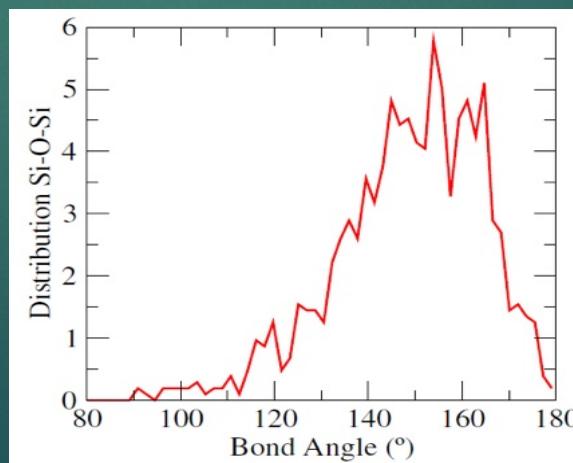
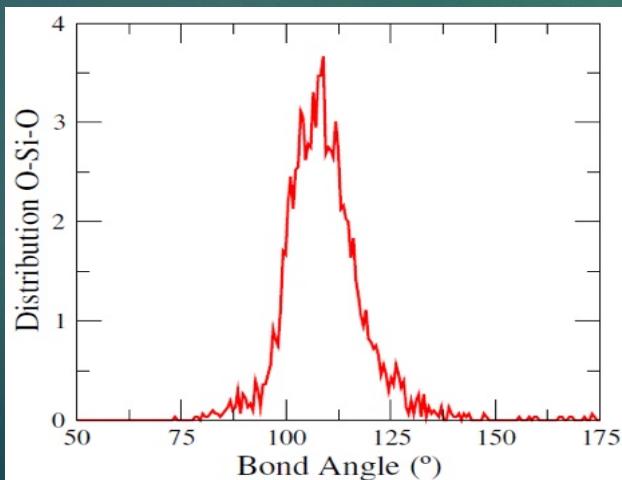


FEAR: minimization of error vs. experiment and total energy.

# Results: silica



| Peak position ( $\text{\AA}$ ) |      |      |                   |
|--------------------------------|------|------|-------------------|
| atom-atom                      | FESR | MD   | Expt.             |
| Si-Si                          | 3.15 | 3.10 |                   |
| Si-O                           | 1.62 | 1.62 | $1.610 \pm 0.050$ |
| O-O                            | 2.64 | 2.64 | $2.632 \pm 0.089$ |



| Bond Angle ( $^\circ$ ) |                 |               |             |              |
|-------------------------|-----------------|---------------|-------------|--------------|
|                         | FESR            | MD            | Expt.       | DR           |
| $O-Si-O$                | 109.5<br>(15.6) | 109.6<br>(10) | 109.5       | 109.5<br>(9) |
| $Si-O-Si$               | 154.3<br>(27.8) | 142.0<br>(25) | 144<br>(38) | 140<br>(25)  |

# Ab initio FEAR – use DFT (VASP or SIESTA) as energy functional

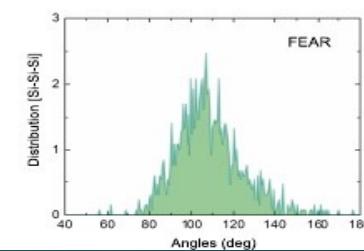
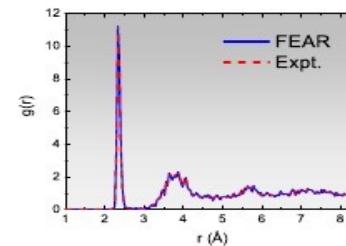
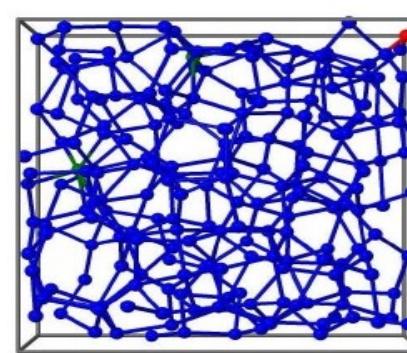
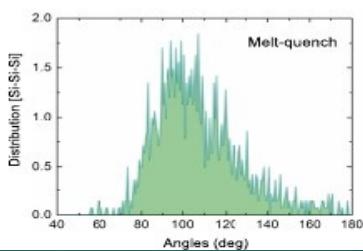
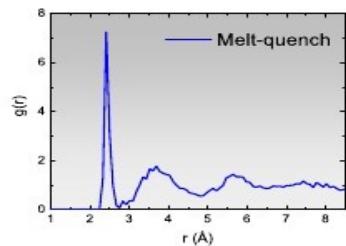
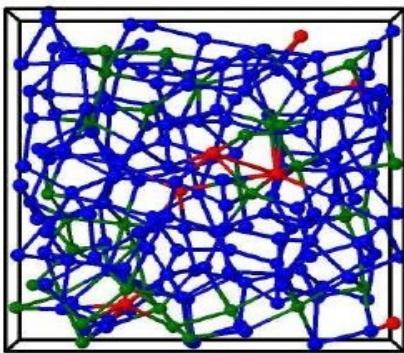
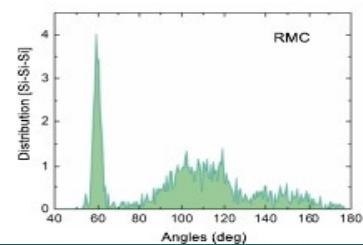
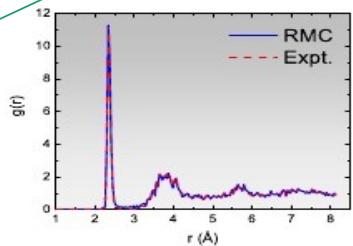
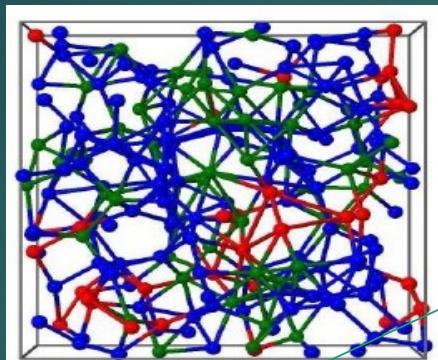
Key to making a general method – to structurally invert a very wide range of materials from diffraction – need general accurate interatomic interactions to unbiased provide chemical information.

First example: silicon and SIESTA

# RMC Melt Quench FEAR

RMC

Melt-Quench



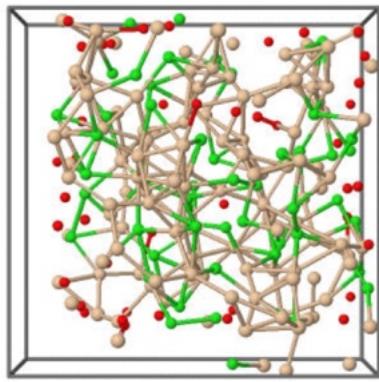
Blue: 4-fold  
Green, Red are  
coordination  
defects

FEAR

# FEAR: a-Si animation and details

## Force-enhanced Atomic Refinement:

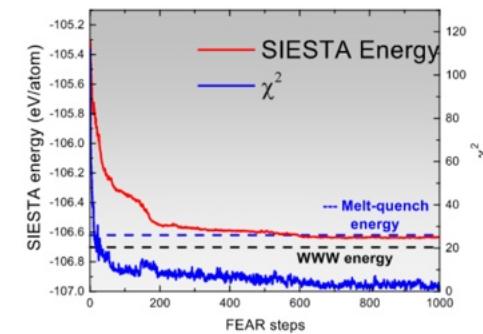
Evolution of 216-atom model amorphous Si starting from random initial configuration with beige sphere representing (correctly coordinated) four-fold atoms, green over-coordinated and red under-coordinated.



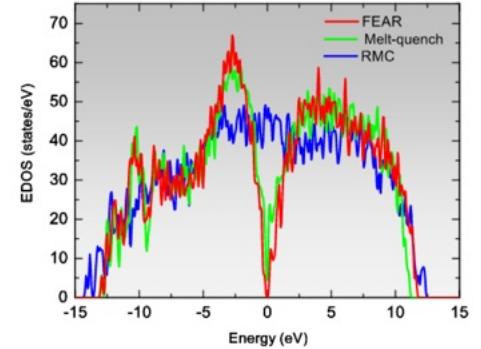
RED : Si (<4)

GREEN : Si (>4)

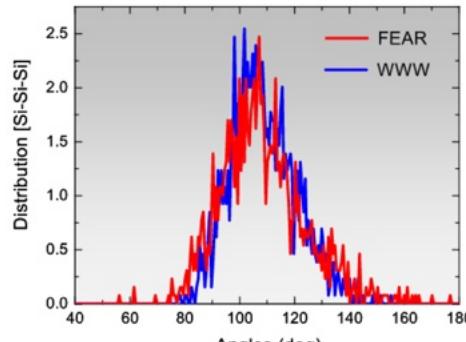
BEIGE : Si (=4)



a)



b)



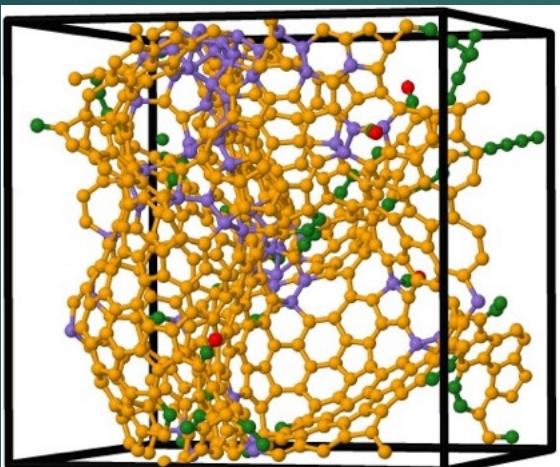
c)

# Example: Amorphous carbon across densities

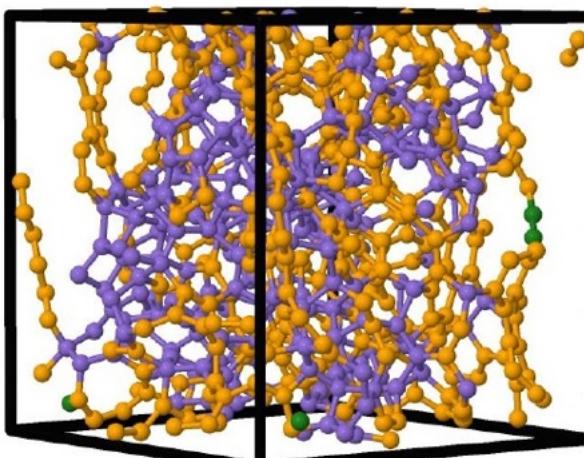
- ▶ Hard: Carbon happily  $sp^3$ ,  $sp^2$  or even  $sp$  bonds. Need a good potential.
- ▶ Wealth of experiments to check against.
- ▶ We carry this out with largish models (up to 800 atoms), SIESTA as energy functional. Then relax final models with VASP (little change).

# Amorphous Carbon across densities

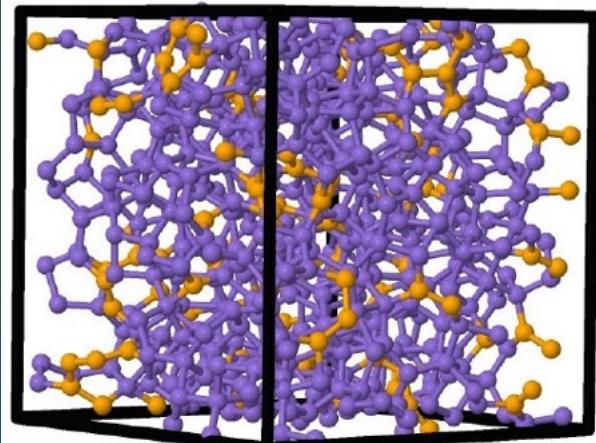
648 atoms



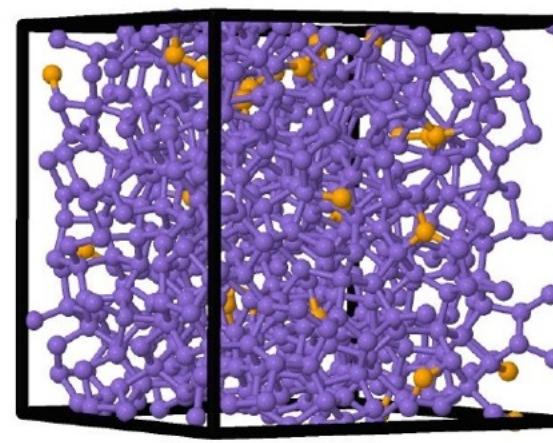
$$\rho = 0.95 \text{ g/cm}^3$$



$$\rho = 2.44 \text{ g/cm}^3$$



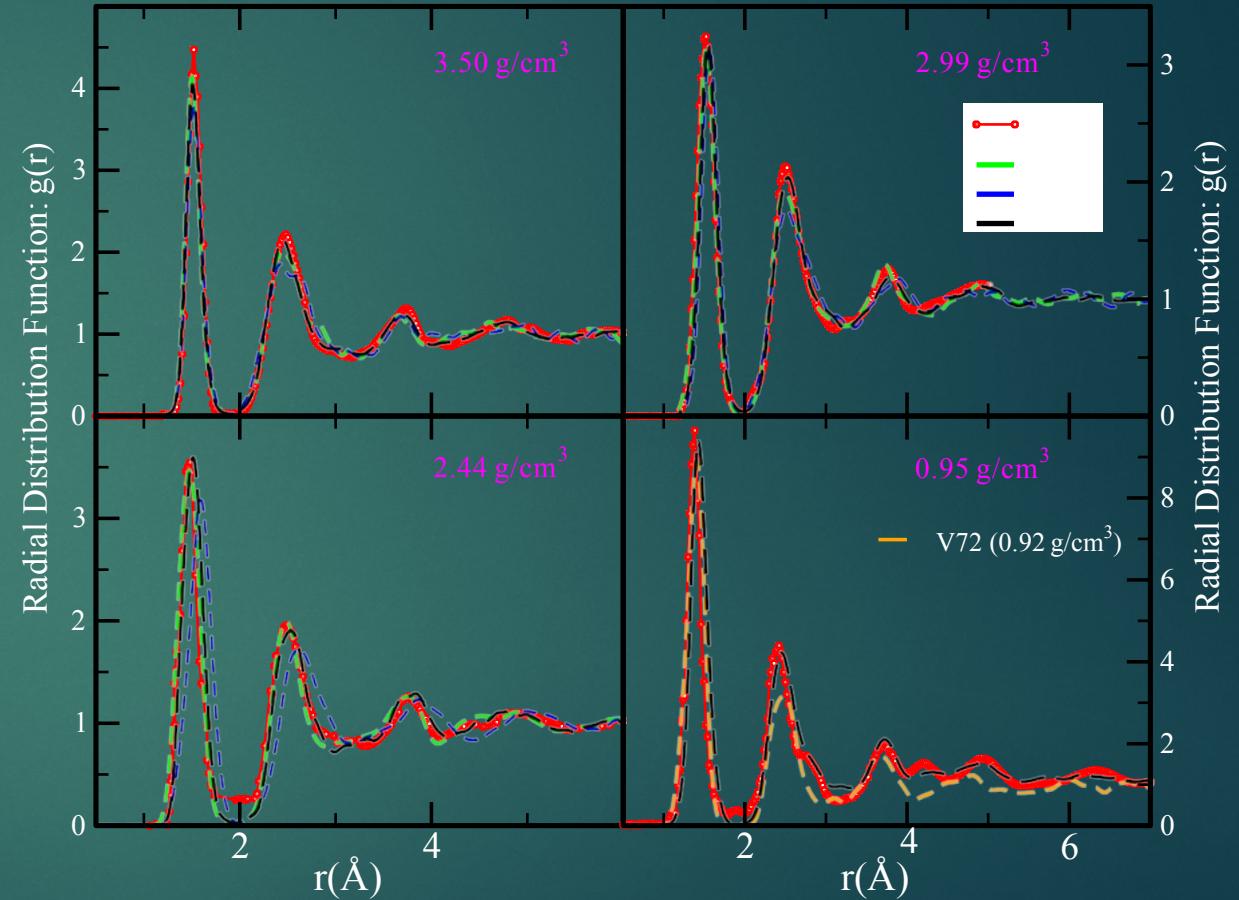
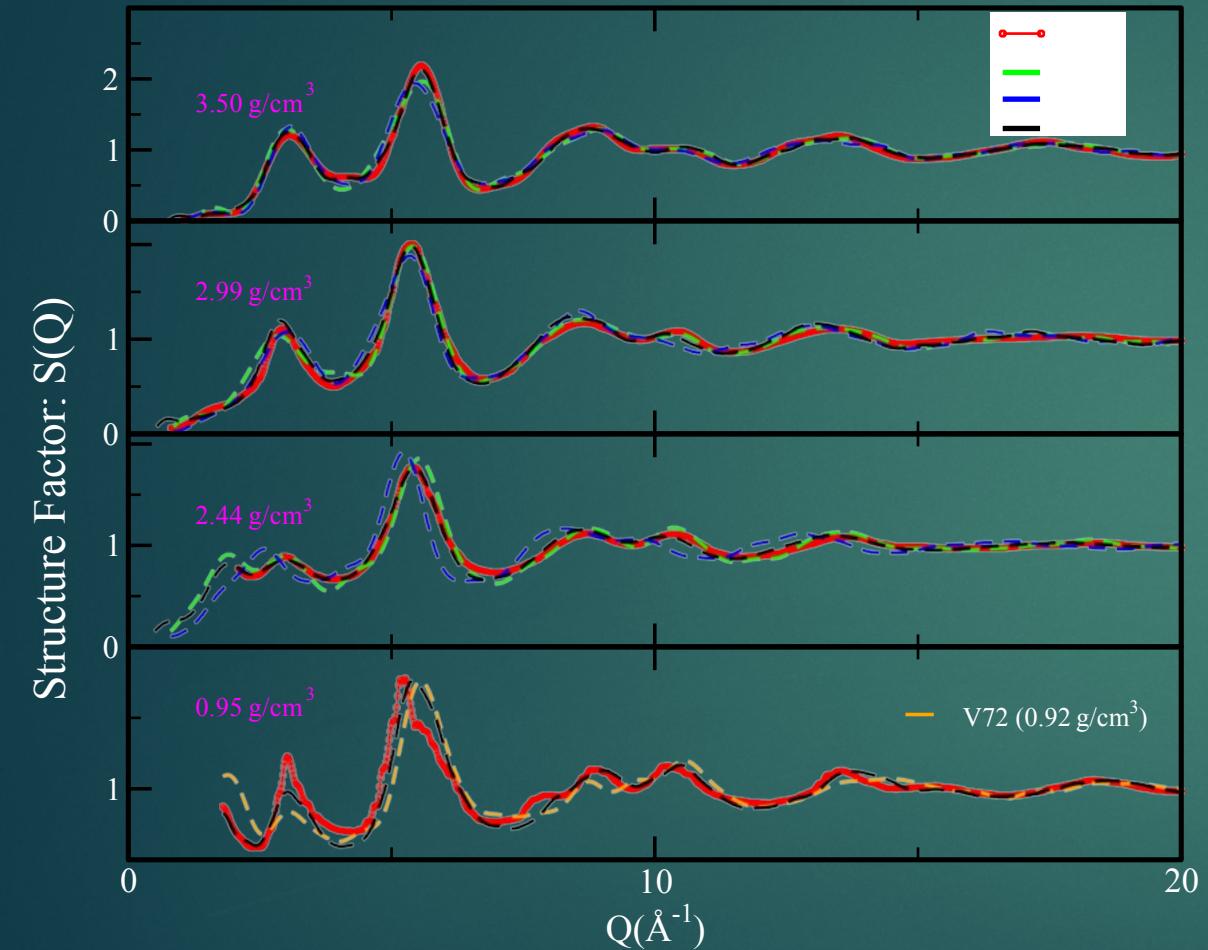
$$\rho = 2.99 \text{ g/cm}^3$$



$$\rho = 3.50 \text{ g/cm}^3$$

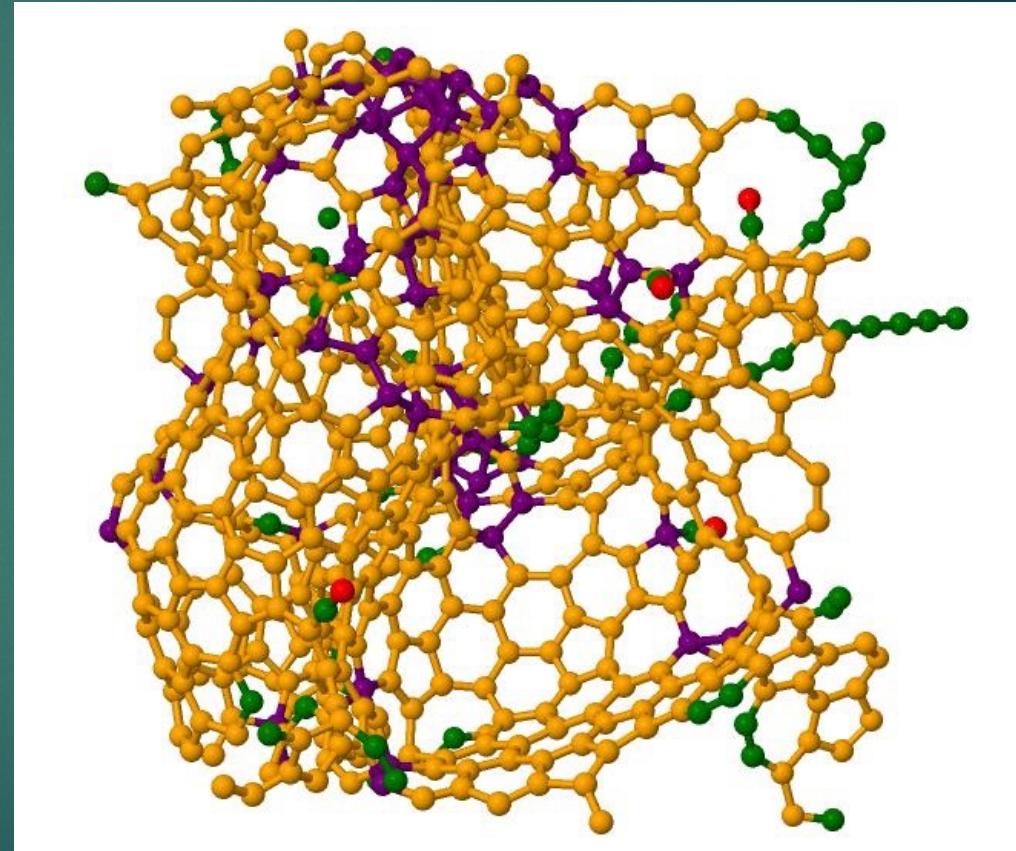
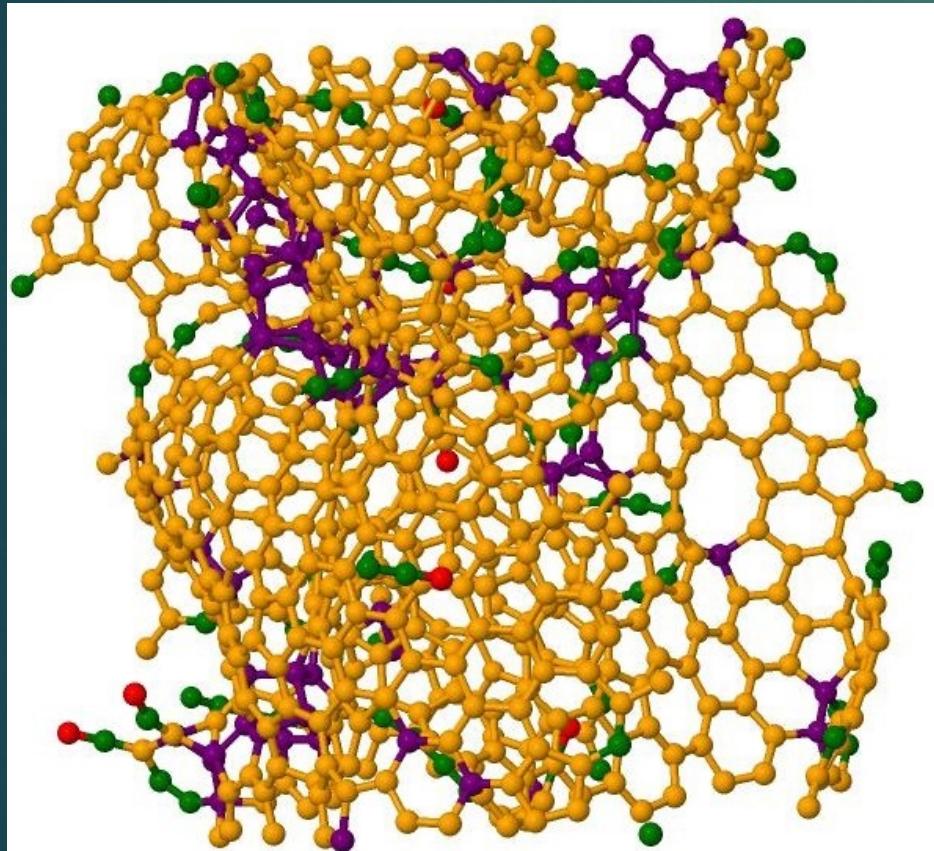
Purple  
( $sp^3$ ),  
Orange  
( $sp^2$ ),  
Green  
( $sp$ )

# Amorphous Carbon

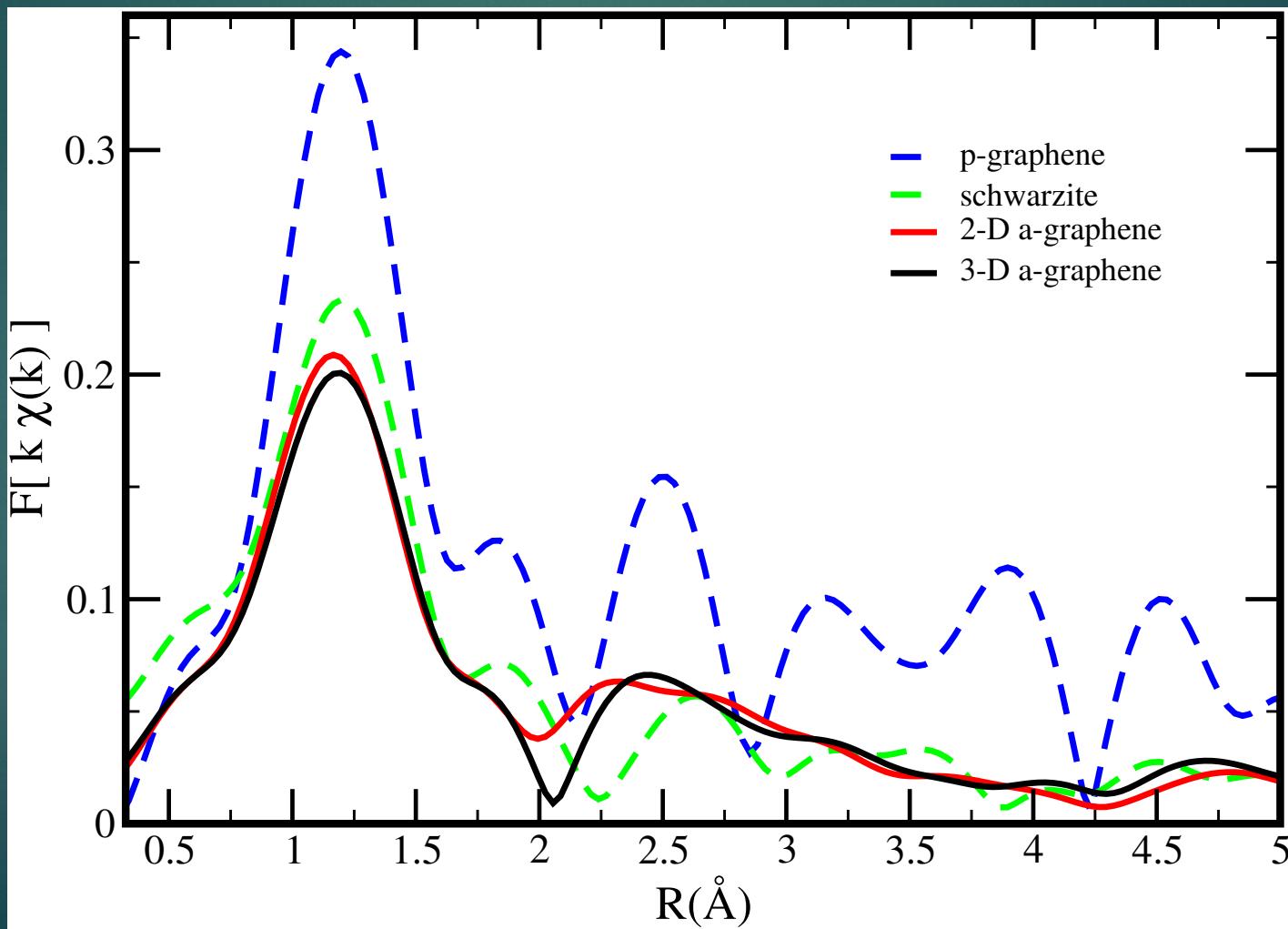


# Low density (0.95 gm/cc) FEAR Carbon (800-, 648-atom models)

Purple ( $sp^3$ ), Orange ( $sp^2$ ), Green ( $sp$ )



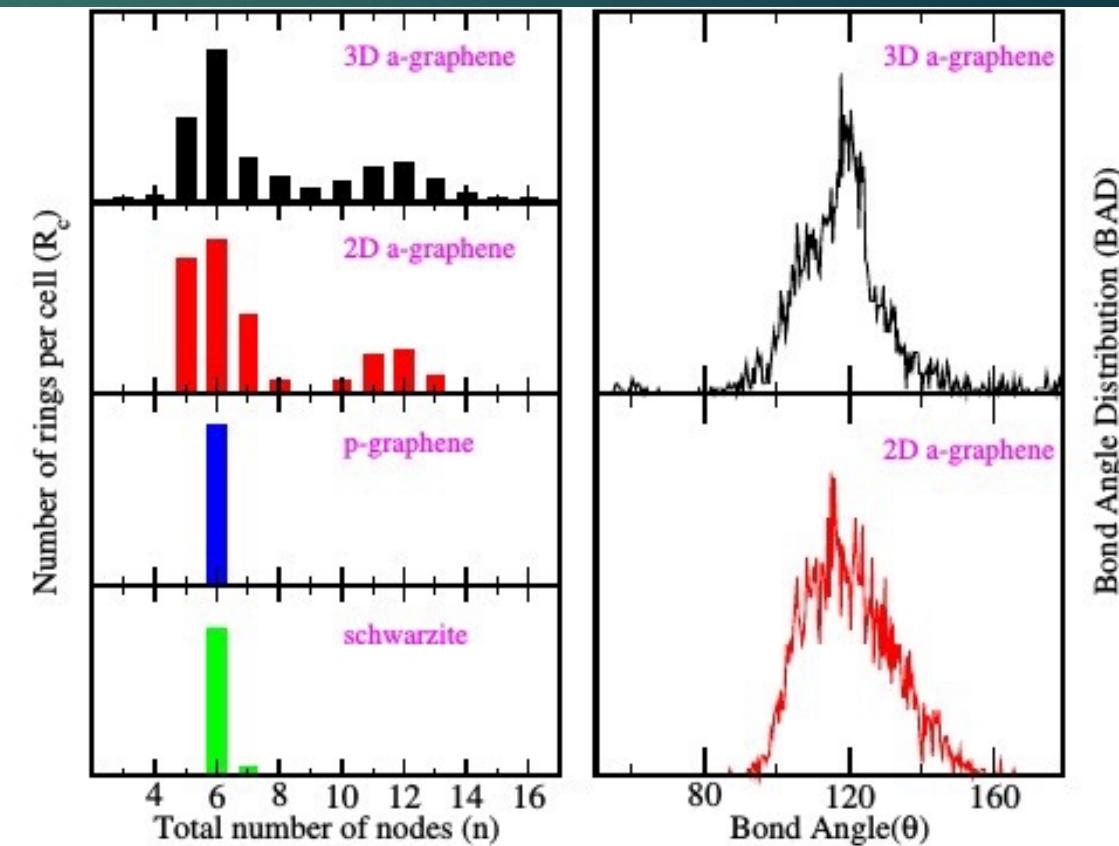
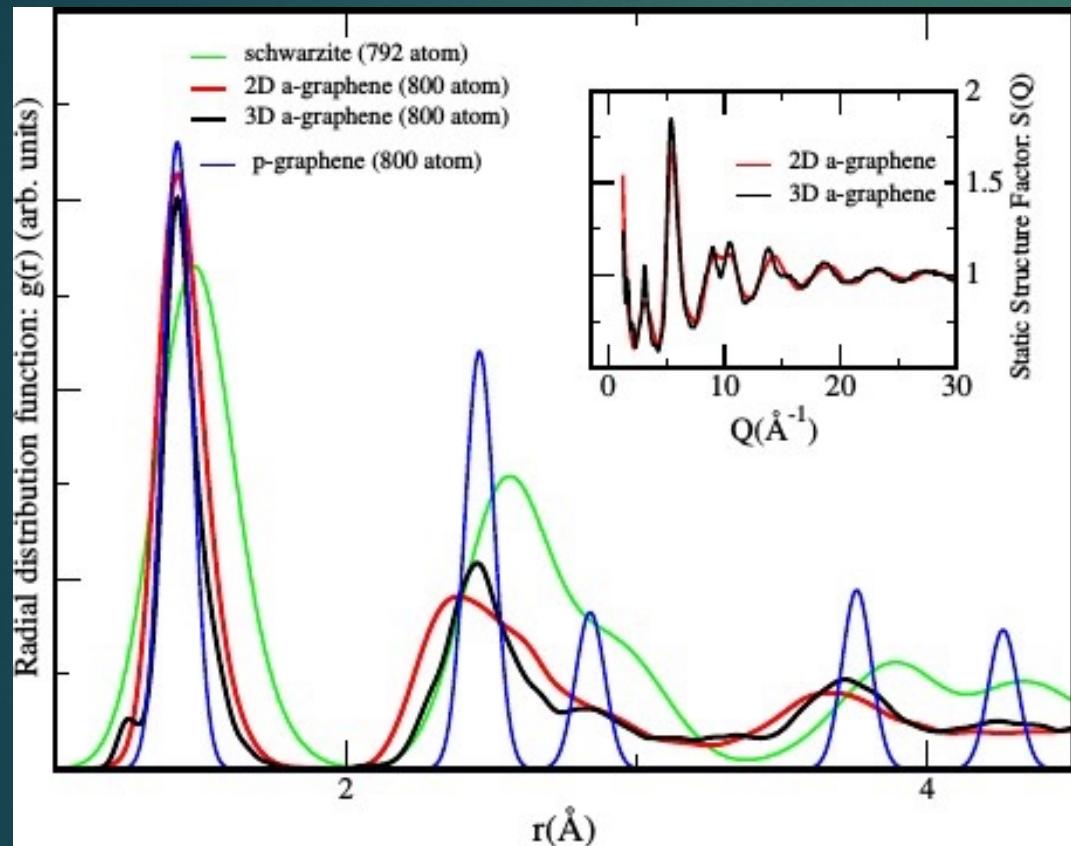
A prediction: EXAFS of 0.95gm/cc  
a-C. Fairly small differences...



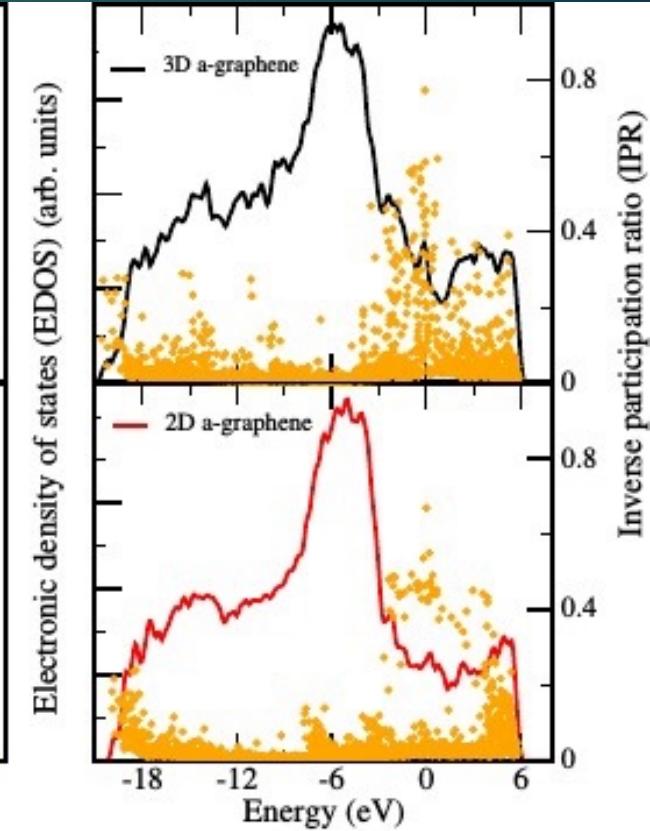
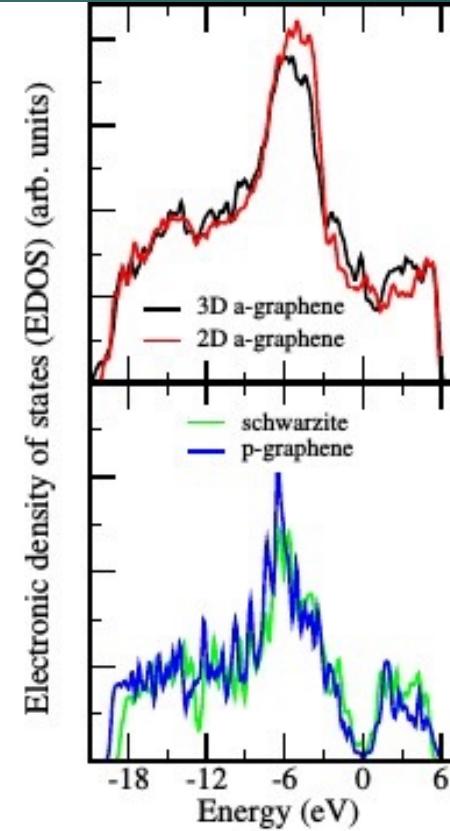
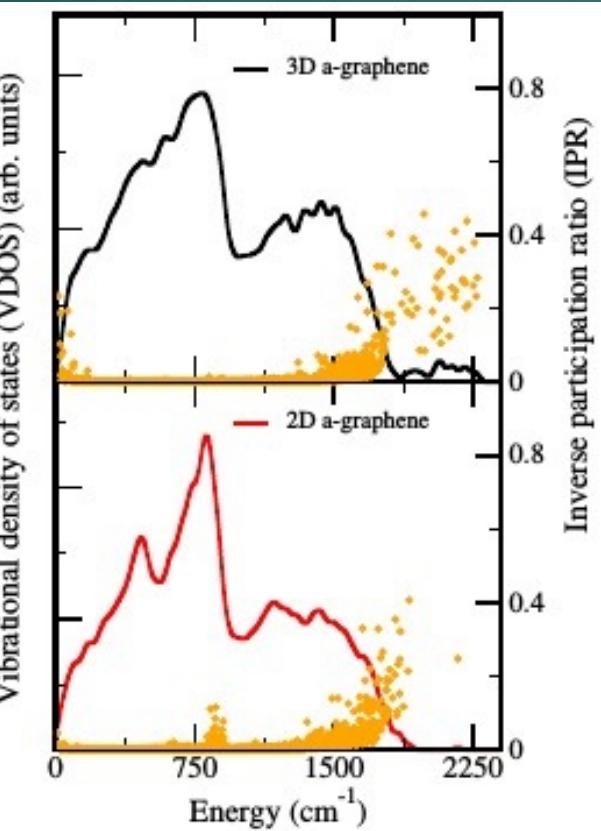
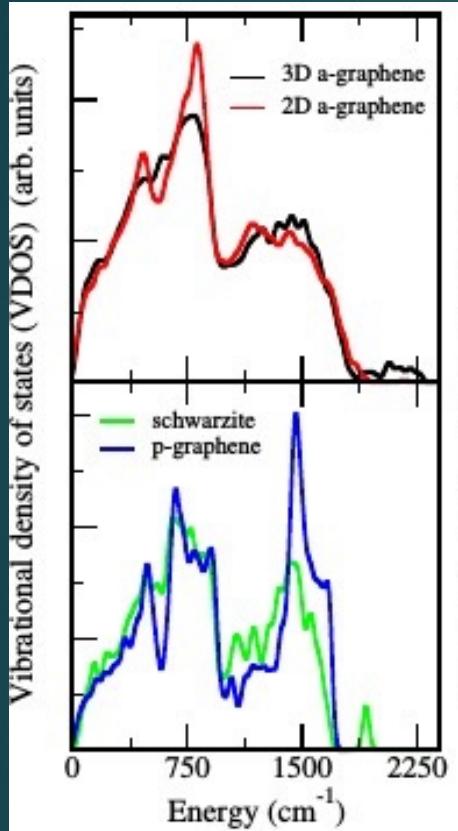
# Comment

- ▶ Amorphous C with density near 1 gm/cc is a form of three-dimensional graphene: warped, wrapped  $sp^2$  sheets including ring disorder (pentagons, hexagons, heptagons) and also with  $sp$  and  $sp^3$  defects.

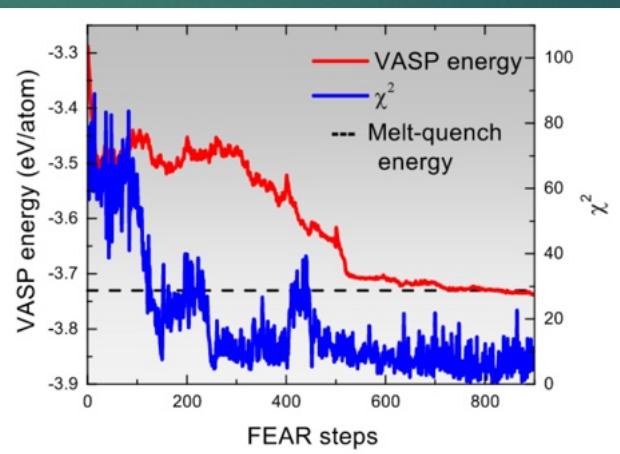
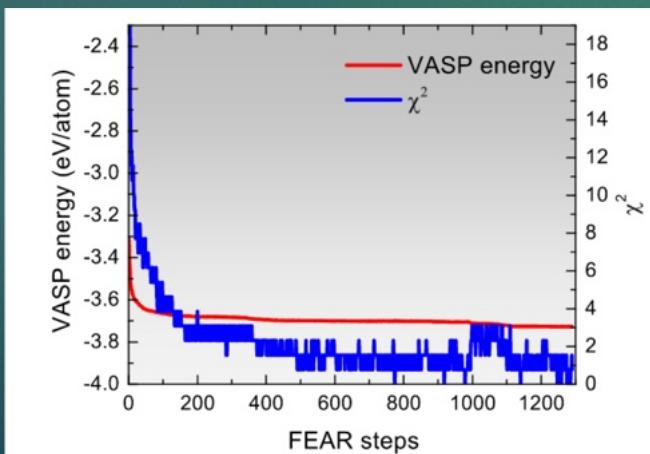
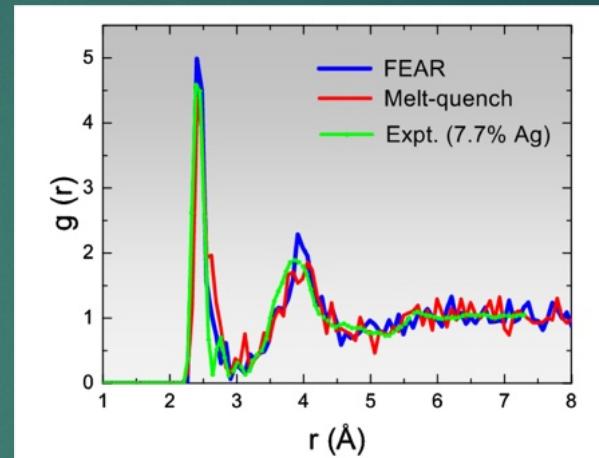
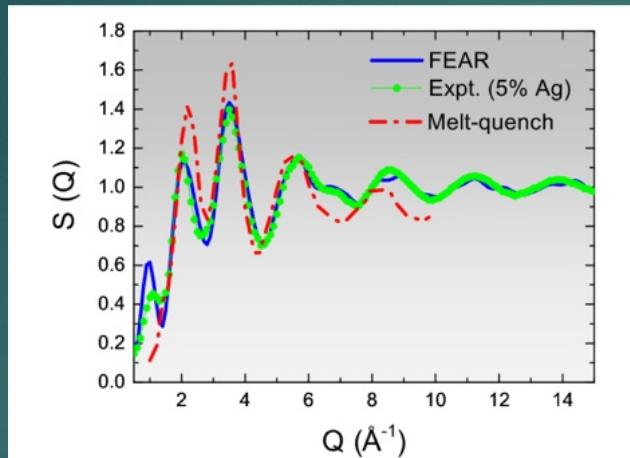
# Structural Comparison



# Electronic and Vibrational Properties



FEAR: Ag-doped chalcogenides,  $[(\text{GeSe}_3)_{1-x}\text{Ag}_x]$   
 $x=0.05, 0.077$  data: Zeidler and Salmon (Bath) VASP,  
A. Pradel group (Montpellier)



# Conclusion (FEAR)

- Efficient: Fewer calls to force code.
- Robust convergence: Really works [a-Si, a-C (0.95-3.5 gm/cc), GeSeAg materials]. We're trying a metallic glass, fiddling with EXAFS too –  $\text{Pd}_{40}\text{Ni}_{40}\text{P}_{20}$  (nothing to report yet!). Used empirical pots, tight-binding, SIESTA and VASP. Routinely produces (slightly) lower total energies than a reasonable melt quench.
- Easy: if you know RMC and VASP, this is essentially a shell script.
- It is GENERAL.